

CS 173, Spring 2016

Examlet 7, Part B

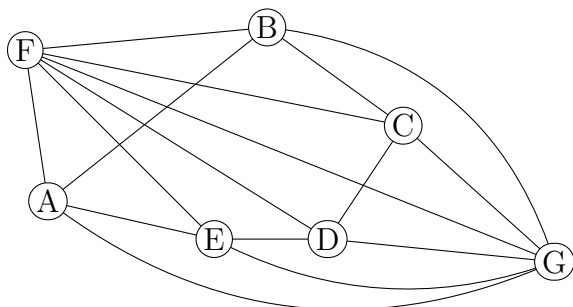
NETID:

FIRST:

LAST:

Discussion: Monday 9 10 11 12 1 2 3 4 5

1. (9 points) What is the chromatic number of graph G (below)? Justify your answer.



2. (6 points) Check the (single) box that best characterizes each item.

$$\sum_{k=3}^n k^7$$

$$\sum_{p=1}^{n-2} p^9 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} (p+2)^7 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} k^9 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} k^7 \quad \boxed{\phantom{0}}$$

Suppose I want to estimate  $\frac{103}{20}$ .  
10 is \_\_\_\_\_

an upper bound

<input type="checkbox"/>
<input type="checkbox"/>

an exact answer

<input type="checkbox"/>
<input type="checkbox"/>

a lower bound

not a bound on

The chromatic number of  $W_n$ .

2 ☐

3 ☐

$\leq 3$  ☐

$\leq 4$  ☐

CS 173, Spring 2016

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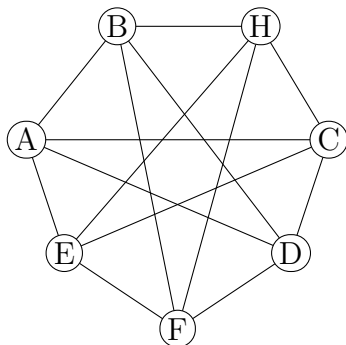
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Discussion: Monday 9 10 11 12 1 2 3 4 5

1. (9 points) What is the chromatic number of graph G (below)? Justify your answer.



2. (6 points) Check the (single) box that best characterizes each item.

$$\sum_{k=0}^n \frac{1}{2^k}$$

$$1 - \left(\frac{1}{2}\right)^{n-1} \quad \boxed{\phantom{00}}$$

$$2 - \left(\frac{1}{2}\right)^n \quad \boxed{\phantom{00}}$$

$$1 - \left(\frac{1}{2}\right)^n \quad \boxed{\phantom{00}}$$

$$2 - \left(\frac{1}{2}\right)^{n-1} \quad \boxed{\phantom{00}}$$

All elements of  $M$  are also elements of  $X$ .

$$M = X \quad \boxed{\phantom{00}}$$

$$M \subseteq X \quad \boxed{\phantom{00}}$$

$$X \subseteq M \quad \boxed{\phantom{00}}$$

Chromatic number of a bipartite graph with at least two vertices.

$$1 \quad \boxed{\phantom{00}}$$

$$2 \quad \boxed{\phantom{00}}$$

$$3 \quad \boxed{\phantom{00}}$$

$$\text{can't tell} \quad \boxed{\phantom{00}}$$

CS 173, Spring 2016  
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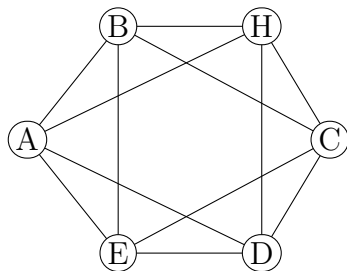
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1. (9 points) What is the chromatic number of graph  $G$  (below)? Justify your answer.



2. (6 points) Check the (single) box that best characterizes each item.

Chromatic number of  $G$      $\mathcal{C}(G)$     ☐     $\phi(G)$     ☐     $\chi(G)$     ☐     $\| G \|$     ☐

$\sum_{k=1}^n \frac{1}{2^k}$      $1 - (\frac{1}{2})^{n-1}$     ☐     $2 - (\frac{1}{2})^n$     ☐     $1 - (\frac{1}{2})^n$     ☐     $2 - (\frac{1}{2})^{n-1}$     ☐

All elements of  $X$  are also elements of  $M$ .     $M = X$     ☐     $M \subseteq X$     ☐     $X \subseteq M$     ☐

CS 173, Spring 2016

Examlet 7, Part B

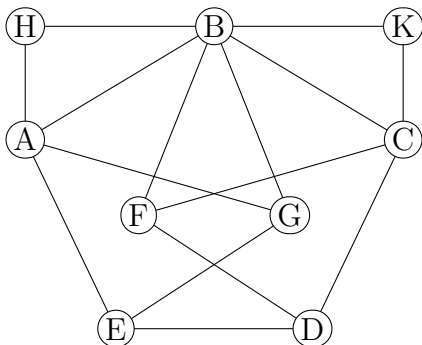
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Discussion: Monday 9 10 11 12 1 2 3 4 5

1. (9 points) What is the chromatic number of graph G (below)? Justify your answer.



2. (6 points) Check the (single) box that best characterizes each item.

10 people rowed across Lake Tahoe in my canoe. 10 is \_\_\_\_\_ how many people the canoe can carry.

an upper bound on  
a lower bound on

☐  
☐

exactly  
not a bound on

☐  
☐

$$\sum_{i=1}^{p-1} i$$

$$\frac{p(p-1)}{2}$$

☐

$$\frac{(p-1)^2}{2}$$

☐

$$\frac{p(p+1)}{2}$$

☐

$$\frac{(p-1)(p+1)}{2}$$

☐

The chromatic number of a graph with maximum vertex degree  $D$

$$= D$$

☐  
☐

$$\leq D + 1$$

$$= D + 1$$

☐  
☐

$$\geq D + 1$$

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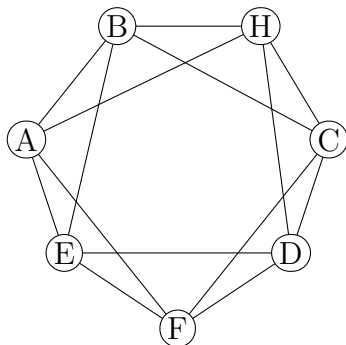
**NETID:**

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**LAST:**

**Discussion:   Monday   9   10   11   12   1   2   3   4   5**

1. (9 points) What is the chromatic number of graph  $G$  (below)? Justify your answer.



2. (6 points) Check the (single) box that best characterizes each item.

Leal team's bridge held 100 pounds without collapsing. 100 pounds is \_\_\_\_\_ on how much the bridge can hold.

an upper bound on

☐

exactly

☐

a lower bound on

☐

not a bound on

☐

$$\sum_{k=3}^n k^7$$

$$\sum_{p=1}^{n-2} p^9 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} k^7 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} k^9 \quad \boxed{\phantom{0}}$$

$$\sum_{p=1}^{n-2} (p+2)^7 \quad \boxed{\phantom{0}}$$

Graph  $H$  is a subgraph of  $W_7$ . 4 is a \_\_\_\_\_ the chromatic number of  $H$ .

an upper bound on

☐

exactly

☐

a lower bound on

☐

not a bound on

☐

# CS 173, Spring 2016

## Examlet 7, Part B

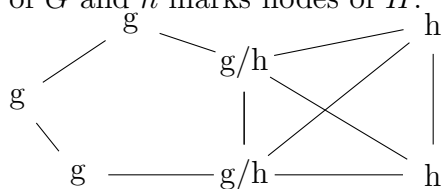
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1. (11 points) If  $G$  is a graph, recall that  $\chi(G)$  is its chromatic number. Suppose that  $G$  is a graph with at least one edge and  $H$  is another graph with at least one edge, not connected to  $G$ . Now, pick a specific edge  $e$  from  $G$  and an edge  $f$  from  $H$  and merge the two edges, creating a combined graph  $T$ . For example, suppose that  $G$  is  $C_5$  and  $H$  is  $K_4$ . Then  $T$  might look as follows, where  $g$  marks nodes of  $G$  and  $h$  marks nodes of  $H$ .



Describe how  $\chi(T)$  is related to  $\chi(G)$  and  $\chi(H)$ , justifying your answer.

2. (4 points) Check the (single) box that best characterizes each item.

$$\sum_{k=0}^{n-1} \frac{1}{2^k}$$

$$1 - \left(\frac{1}{2}\right)^{n-1}$$

☐

$$2 - \left(\frac{1}{2}\right)^n$$

☐

$$1 - \left(\frac{1}{2}\right)^n$$

☐

$$2 - \left(\frac{1}{2}\right)^{n-1}$$

☐

$$\tau \leq 1.3$$

an upper bound on  $\tau$

☐  
☐

a lower bound on  $\tau$

exactly  $\tau$

☐  
☐

not a bound on  $\tau$