| CS 173, Sp<br>Examlet 12                                    | •                 | NETI              | ID:                         |                  |                  |                                |        |                |                    |   |        |  |
|---|-------------------|-------------------|-----------------------------|------------------|------------------|--------------------------------|--------|----------------|--------------------|---|--------|--|
| FIRST:  |                   |                   |                             | LAS              | Γ:               |                                |        |                |                    |   |        |  |
| Discussion:   | Monday            | 9 10              | 11                          | 12               | 1                | 2                              | 3      | 4              | 5                  |   |        |  |
| (9 points) Let $f$ define its image $f$ aformally explain w | f(S) by $f(S) =$  | $\{f(s)\in Y$     | $Y \mid s \in$              | $S$ }. Is        | it the           | e case                         | e that | f(A)           | $(1) \cap j$       | r(B) =                                  | = f(A) |  |
|   |                   |                   |                             |                  |                  |                                |        |                |                    |   |        |  |
|   |                   |                   |                             |                  |                  |                                |        |                |                    |   |        |  |
|   |                   |                   |                             |                  |                  |                                |        |                |                    |   |        |  |
| (6 points) Check  | the (single) box  | x that best       | t charac                    | cterizes         | each i           | tem.                           |        |                |                    |   |        |  |
| How many ways of among 10 varieties number of bagels        | es, if I can have | any               | 10!<br>5!5!<br>15!<br>10!5! |                  | $\overline{10}$  | 14!<br>0!4!<br>10 <sup>5</sup> |        | (              | 14!<br>0!5!        |   |        |  |
| Pascal's identity that $\binom{n+1}{k}$ is equal            | _                 | $+\binom{n}{k+1}$ |                             | $\binom{n}{k}$ + | $\binom{n-1}{k}$ |                                |        | $\binom{n}{k}$ | $+$ $\binom{k}{k}$ | $\begin{pmatrix} n \\ -1 \end{pmatrix}$ |        |  |
| If $f: \mathbb{R} \to \mathbb{P}(\mathbb{Z})$ t             | hen $f(17)$ is    | one (             |                             | n intege         |                  |                                | a se   |                | integ<br>ower      | Γ                                       |        |  |

infinite

| Discussion: Monday 9 1  Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ Let $f: \mathbb{R}^2 \to \mathbb{P}(\mathbb{R}^2)$ be defined by $f(x,y) = 1$ | 10 11 12 1 2 3 4 5 $\{(p,q) \in \mathbb{R}^2 \mid (p-x)^2 + (q-y)^2 = 4\}$ |
|---|--|
| Let $T = \{ f(x, y) \mid (x, y) \in \mathbb{R}^2 \}.$   | $\{(p,q) \in \mathbb{R}^2 \mid (p-x)^2 + (q-y)^2 = 4\}$                    |
| (6 points) Answer the following question  |  |
|   | ns:  |
| Describe (at a high level) the elements of  | of $f(3,5)$ :  |
| $f(0,0) \cap f(0,4) =$  |  |
| The cardinality of (aka the number of el  | lements in) $T$ is:  |
| (7 points) Is $T$ a partition of $\mathbb{R}^2$ ? For each why $T$ does or doesn't satisfy that condition   | ch of the conditions required to be a partition, briefly explain.          |
|   |  |
|   |  |

 $|\{A \subseteq \mathbb{Z}_4 : |A| \text{ is even}\}|$ 

| FIRST:   |   |                         | LAS   | <b>T:</b>  |             |           |                  |
|--|---|-------------------------|---|------------|-------------|-----------|------------------|
| Discussion:  | Monday  | 9 10                    | $egin{array}{c c} & & & \\ \hline 11 & 12 & & \\ \end{array}$ | 1 2        | 3 4         | 5         |                  |
| Graph $G$ is at rig $V$ is the set of no                           | ght. (A   |                         | [I  |            | E           | F         | ©                |
| Define $f: V \to \mathbb{P}(V)$<br>Let $P = \{f(p) \mid p \in V\}$ | $\begin{cases} f(p) & \text{if } p \\ V \end{cases}.$ | $\in V : \deg(n)$       | $d(p) \le \deg(p)$  | , where de | eg(n) is th | e degree  | of node n.       |
| (6 points) Fill in   |   | alues:                  |   |            |             |           |                  |
| f(A) =   | 0   |                         |   |            |             |           |                  |
| ( )  |   |                         |   |            |             |           |                  |
| f(C) =   |   |                         |   |            |             |           |                  |
| P =  |   |                         |   |            |             |           |                  |
| (7 points) Is $P$ a why $P$ does or does                           |   |                         | the condition   | ns require | d to be a   | partition | , briefly explai |
|  |   |                         |   |            |             |           |                  |
|  |   |                         |   |            |             |           |                  |
|  |   |                         |   |            |             |           |                  |
|  |   |                         |   |            |             |           |                  |
|  |   |                         |   |            |             |           |                  |
| (2 points) Check   | the (single) bo                                       | x that best c           | haracterizes  | each item  |             |           |                  |
| For all sets $A$ and   | $d B, \mathbb{P}(A \cap B) \subseteq$                 | $\mathbb{P}(A \cup B).$ | always  | SC         | ometimes    |           | never            |

| CS 173, Spring<br>Examlet 12, P                                 |                     | ETID:                |          |                |       |               |             |                        |          |
|---|---------------------|----------------------|----------|----------------|-------|---------------|-------------|------------------------|----------|
| FIRST:  |                     |                      | LAS'     | T:             |       |               |             |                        |          |
|   | onday 9             |                      |          | 1              |       |               | 4 5         |                        |          |
| (9 points) Define $f : \mathbb{Z}$ nat $k p$ . Compare $f(r,k)$ |                     |                      |          | $\mathbb{Z}:x$ | = y - | + <i>kn</i> 1 | for som     | $e \ n \in \mathbb{Z}$ | . Suppos |
|   |                     |                      |          |                |       |               |             |                        |          |
|   |                     |                      |          |                |       |               |             |                        |          |
|   |                     |                      |          |                |       |               |             |                        |          |
|   |                     |                      |          |                |       |               |             |                        |          |
|   |                     |                      |          |                |       |               |             |                        |          |
|   |                     |                      |          |                |       |               |             |                        |          |
| (6 points) Check the (si  | ingle) box that     | best chara           | cterizes | each it        | tem.  |               |             |                        |          |
| A partition of a set A c  | ontains $\emptyset$ | al                   | ways     |                | som   | $_{ m etime}$ | s           | neve                   | er       |
| How many ways can I ch  | _                   | om $\frac{8!}{6!2!}$ |          | 13!<br>6!7!    |       |               | 14!<br>9!5! |                        |          |
| among 8 varieties, if I con number of bagels from a             |                     | <u>14!</u><br>6!7!   |          | $8^{6}$        | i     |               | 68          |                        |          |
| If $f: \mathbb{N} \to \mathbb{P}(\mathbb{Q})$ then $f$          | (3) is              | a r                  | ational  |                | a     | powe          | r set of    | rationals              | 5        |
| , ( <del>(</del> ) 011011                                       |                     | a set of ra          | tionals  |                |       |               | ι           | ındefined              |          |

| FIRST:   |                |        |        |         | LAS       | <b>T</b> : |        |        |        |         |         |            |
|--|----------------|--------|--------|---------|-----------|------------|--------|--------|--------|---------|---------|------------|
| Discussion:  | Monday         | 9      | 10     | 11      | 12        | 1          | 2      | 3      | 4      | 5       |         |            |
| Graph $G$ is at right $V$ is the set of node $M = \{0, 1, 2, 3, 4\}$ | <i>(</i> ,     |        |        | B       | Ē         |            |        |        | Ē      | F       |         | C          |
| Define $f: M \to \mathbb{P}(V)$ between $a$ and $b$ . Let            |                |        |        | (p, F)  | $=n$ }, v | where      | d(a,   | b) is  | the (s | shortes | st-path | n) distanc |
| (6 points) Fill in th  | ne following v | alues: |        |         |           |            |        |        |        |         |         |            |
| f(0) =   |                |        |        |         |           |            |        |        |        |         |         |            |
| f(1) =   |                |        |        |         |           |            |        |        |        |         |         |            |
| P =  |                |        |        |         |           |            |        |        |        |         |         |            |
| (7 points) Is $P$ a pay  |                |        |        | f the c | conditio  | ns req     | quired | l to b | e a pa | artitio | n, brie | fly explai |
|  |                |        |        |         |           |            |        |        |        |         |         |            |
|  |                |        |        |         |           |            |        |        |        |         |         |            |
|  |                |        |        |         |           |            |        |        |        |         |         |            |
|  |                |        |        |         |           |            |        |        |        |         |         |            |
| (2 points) Check th  | ne (single) bo | x that | t best | charac  | cterizes  | each :     | item.  |        |        |         |         |            |
| Let $A$ be a non-em  | pty set.       |        |        |         |           |            |        |        |        |         |         |            |
| $\{A\}$ is a partition of  | - •            |        |        | alwa    | vs        |            | some   | timos  | ,      | 7       | never   |            |

always

sometimes

never

| DIDOM  |                      |         |        |              | TAGG       | Π                |                  |      |        |       |         |        |
|--|----------------------|---------|--------|--------------|------------|------------------|------------------|------|--------|-------|---------|--------|
| FIRST:   |                      |         |        |              | LAST       | L' <b>:</b>      |                  |      |        |       |         |        |
| Discussion:  | Monday               | 9       | 10     | 11           | <b>12</b>  | 1                | 2                | 3    | 4      | 5     |         |        |
| (9 points) Recal ments that are in of integers $A$ , let | one of the two       | sets bu | ut not | the o        | ther. The  |                  |                  |      |        |       |         |        |
| Explain clearly w  |                      |         |        |              |            | $[\mathbb{Z}] =$ | $[\mathbb{N}]$ ? | Brie | fly ju | stify | your an | iswer. |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
|  |                      |         |        |              |            |                  |                  |      |        |       |         |        |
| (6 points) Check   | the (single) box     | x that  | best o | charac       | eterizes o | each             | item.            |      |        |       |         |        |
| (0)  | , ,                  |         |        |              |            |                  |                  |      |        |       |         |        |
| (0)  | -1                   | )       | ] .    | 1            | 2          |                  |                  | und  | efine  | ed _  |         |        |
| $\mathbb{P}(A \cup B) = \mathbb{P}(A)$                   | $\cup \mathbb{P}(B)$ | 8       | always |              | SO         | meti             | mes              |      |        | never |         |        |
| If you want to take out of 35 classes                    |                      |         |        | 35!<br>31!4! |            | 3                | $5^4$            |      |        |       |         |        |
| different choices  |                      |         | J      | 35!<br>31!   |            |                  |                  |      |        |       |         |        |