NetID:_____ Lecture: A B

Discussion: Thursday Friday 9 10 11 12 1 2 3 4 5 6

(10 points) Suppose we have a function f defined by

$$f(0) = f(1) = 3$$

 $f(n) = 5f(n-2) + d$, for $n \ge 2$

where d is a constant. Your partner has already figured out that

$$f(n) = 5^k f(n - 2k) + \sum_{p=0}^{k-1} d5^p$$

Finish finding the closed form for f(n) assuming that n is even. Show your work and simplify your answer. Recall the following useful closed form (for $r \neq 1$): $\sum_{k=0}^{n} r^k = \frac{r^{n+1}-1}{r-1}$

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Discussion: Friday 9 **12** 1 $\mathbf{2}$ 3 Thursday 10 11 4 5 6

1. (8 points) Suppose we have a function f defined by

$$f(0) = f(1) = 3$$

 $f(n) = 5f(n-2) + d$, for $n \ge 2$

where d is a constant. Express f(n) in terms of f(n-6) (where $n \geq 6$). Show your work and simplify your answer. You do **not** need to find a closed form for f(n).

2. (2 points) Check the (single) box that best characterizes each item.

f(n) = n! can be defined recursively by f(0) = 1, and f(n) = nf(n-1)for all integers ...

 $n \ge 0$ $n \ge 1$ $n \ge 2$

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1. (8 points) Suppose we have a function g defined (for n a power of 3) by

$$g(1) = c$$

$$g(n) = 3g(n/3) + n \text{ for } n \ge 3$$

Express g(n) in terms of $g(n/3^3)$ (where $n \ge 27$). Show your work and simplify your answer. You do **not** need to find a closed form for g(n).

2. (2 points) Suppose that $f: \mathbb{N} \to \mathbb{N}$ is such that $f(n) = n^2$. Give a recursive definition of f

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(10 points) Suppose we have a function g defined (for n a power of 4) by

$$g(1) = c$$

$$g(n) = 2g(n/4) + n \text{ for } n \ge 4$$

Your partner has already figured out that

$$g(n) = 2^k g(n/4^k) + n \sum_{p=0}^{k-1} \frac{1}{2^p}$$

Finish finding the closed form for f(n) assuming that n is a power of 4. Show your work and simplify your answer. Recall that $\log_b n = (\log_a n)(\log_b a)$.

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Discussion: Thursday Friday 9 10 11 12 1 2 3 4 5 6

(10 points) Suppose we have a function g defined (for n a power of 2) by

$$g(1) = c$$

$$g(n) = 4g(n/2) + n \text{ for } n \ge 2$$

Your partner has already figured out that

$$g(n) = 4^k g(n/2^k) + n \sum_{p=0}^{k-1} 2^p$$

Finish finding the closed form for g(n) assuming that n is a power of 2. Show your work and simplify your answer. Recall that $\log_b n = (\log_a n)(\log_b a)$.

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Discussion: Thursday Friday 9 10 11 12 1 2 3 4 5 6

1. (8 points) Suppose we have a function g defined by

$$g(0) = g(1) = c$$

 $g(n) = kg(n-2) + n^2$, for $n \ge 2$

where k and c are constants. Express g(n) in terms of g(n-6) (where $n \ge 6$). Show your work and simplify your answer. You do **not** need to find a closed form for g(n).

2. (2 points) Check the (single) box that best characterizes each item.

The number of nodes in the 4-dimensional hypercube Q_4

4

16

32

64