Name:											
NetID:):				Lecture:			В			
Discussion	Thursday	Friday	10	11	12	1	2	3	4	5	6

(15 points) Professor Martinez needs a state machine that will recognize the sequence 11122 when typed on a keypad. Specifically, it must read any sequence of the digits 0, 1, and 2. It should move into a final state immediately after seeing 11122, and then remain in that final state as further characters come in. For efficiency, the state machine must be deterministic, i.e. if you look at any state s and any action s, there is **exactly** one edge labelled s leaving state s.

Draw a deterministic state diagram that will meet his needs, using no more than 9 states and, if you can, no more than 6.

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(5 points) Let answer.	A be the set of	all relations	on \mathbb{N} .	Is A co	untabl	e or	uncou	intab	le? B	riefly	justify your
The rational	neck the (single) numbers have ity as the reals.			٦	es each	item		ot kno	own		
A product of is countable.	countable sets	true	fal	se] tı	rue f	or fin	ite pr	oduc	ts	
All possibilit could be store top's hard drive	d on your lap-	finite		countab	ly infir	nite		u	ncoui	ntable	,
The set of all numbers.		finite	cot	ıntably	infinit	e [unc	ounta	able	
Every mathen finite formula.	natical function h	as a tru	e	f	alse		no	ot kno	own		

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(5 points) Is t showing that it is	the following claims not.	n true? Infor	mally o	explain	why it	is, o	r give	a cor	ıcrete	e coun	ter-example
Claim: For	all positive intege	$\operatorname{rs} a, b, \text{ and } c$, if gcd((a,b) =	= 1 and §	$\gcd($	b, c) =	= 1, th	nen go	$\mathrm{cd}(a, a)$	c) = 1.
(10:		l 4l -4 l	. .		l.	·					
(10 points) Ci	heck the (single)	box that bes	st chara	acterize	es each	пеп	1.				
$\forall x \in \mathbb{R},$ if $x^2 > 100$, the	nen $ x \ge 10$.	tru	e		false						
$\{1,2\}\cap\emptyset=$	Ø	{	$(1,\emptyset),$	$(2,\emptyset)$			{1,5	$[2,\emptyset]$			
	$\{\emptyset\}$	{	[1, 2]				und	efined	l [
If xRy is nevertation R is	er true, then the	symme both	etric [antis neith		netric				
If a function f it must be one	from \mathbb{R} to \mathbb{R} is in e-to-one.	•	rue [$\mathrm{fals}\epsilon$	e [
	mber of a graph at least one edge	1		2			3		С	an't t	ell

Name:_

NetID: Lecture: A \mathbf{B}

Friday Thursday 1 2 3 Discussion: **10** 11 **12** 4 5 6

(5 points) Suppose that $f: \mathbb{N} \to \mathbb{N}$ is such that $f(n) = n^2$. Give a recursive definition of f

(10 points) Check the (single) box that best characterizes each item.

$$\sum_{k=1}^{n} \frac{1}{2^k}$$

$$2-\left(\frac{1}{2}\right)^n$$

$$1 - (\frac{1}{2})^n$$

$$2 - (\frac{1}{2})^{n-1}$$

Dividing a problem of size n into k subproblems, each of size n/m, has the best big- Θ running time when

$$k = m$$

$$km = 1$$

 3^n is

$$\Theta(5^n)$$

$$O(5^n)$$

neither of these

$$\leq h$$

$$h+1$$

The diameter of a full, complete 7-ary tree of height h.

$$7h+1$$

$$\binom{k}{k-1}$$

undefined