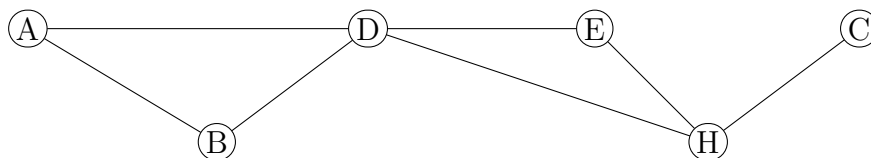


Name: \_\_\_\_\_

NetID: \_\_\_\_\_

Lecture: B

Discussion: Friday 11 12 1 2 3 4

Graph  $G$  is at right. $V$  is the set of nodes in  $G$ . $M = \{0, 1, 2, 3, 4\}$ 

Define  $f : M \rightarrow \mathbb{P}(V)$  by  $f(n) = \{p \in V : d(p, E) = n\}$ , where  $d(a, b)$  is the (shortest-path) distance between  $a$  and  $b$ . Let  $P = \{f(n) \mid n \in M\}$ .

(6 points) Fill in the following values:

 $f(0) =$  $f(1) =$  $P =$ 

(7 points) Is  $P$  a partition of  $V$ ? For each of the conditions required to be a partition, briefly explain why  $P$  does or doesn't satisfy that condition.

(2 points) Check the (single) box that best characterizes each item.

$$\mathbb{P}(A) \cap \mathbb{P}(B) = \mathbb{P}(A \cap B)$$

always

☐

sometimes

☐

never

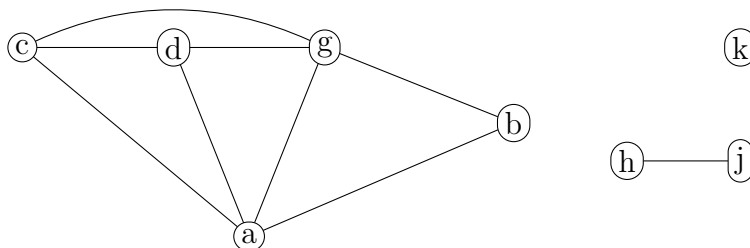
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Name: \_\_\_\_\_

NetID: \_\_\_\_\_

Lecture: B

Discussion: Friday 11 12 1 2 3 4

Graph  $G$  is at right. $V$  is the set of nodes. $E$  is the set of edges. $ab$  (or  $ba$ ) is the edge between  $a$  and  $b$ .Let  $f : V \rightarrow \mathbb{P}(E)$  be defined by  $f(n) = \{e \in E \mid n \text{ is an endpoint of } e\}$ . And let  $T = \{f(n) \mid n \in V\}$ .

(6 points) Fill in the following values:

$|V| =$

$f(d) =$

$f(h) =$

(7 points) Is  $T$  a partition of  $E$ ? For each of the conditions required to be a partition, briefly explain why  $T$  does or doesn't satisfy that condition.(2 points) State the definition of  $\binom{n}{k}$ , i.e. express  $\binom{n}{k}$  in terms of more basic arithmetic operations.