Name:____

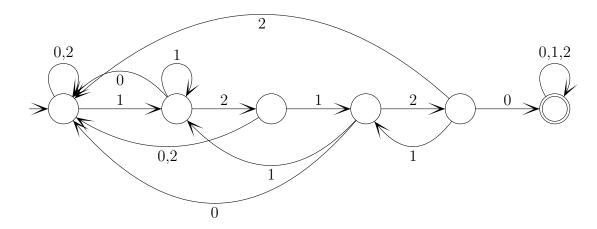
NetID:_____ Lecture: A B

Discussion: Thursday Friday 9 10 11 12 1 2 3 4 5 6

(15 points) Professor Martinez needs a state machine that will recognize the sequence 12120 when typed on a keypad. Specifically, it must read any sequence of the digits 0, 1, and 2. It should move into a final state immediately after seeing 12120, and then remain in that final state as further characters come in. For efficiency, the state machine must be deterministic. Specifically, if you look at any state s and any action a, there is **exactly** one edge labelled a leaving state s.

Draw a deterministic state diagram that will meet his needs, using no more than 9 states and, if you can, no more than 6.

Solution:



Name:												
NetID:			Lecture:			e :	A	В				
Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6
(5 points) Leadistinct (finite) gr	t's say that two graphs countable o	-							mor	phic.	Is the	e set of
Solution: The distinct graphs will is countable.	is set is countable that many noo		-				,					
(10 points) Ch	neck the (single) b	ox that bes	t cha	ıracteri	zes eac	ch item	1.					
$f: \mathbb{N} \to \mathbb{N}$ has $C++$ program	natical function s a corresponding n that will comen an input of n .	true		fals	e 🗸	,	not k	nown				
The rational the same card integers.		true $\sqrt{}$		false		not	knov	wn [
If A is countal is $\mathbb{P}(A)$ counta	bly infinite, then ably infinite?	always] s	ometin	nes [nev	er			
The set of all trees where ea contains one o B, or C	ch node	finite		counta	ably in	finite		u	ncou	onumber intab olimits	le	
The set of all the real line.	intervals $[a, b]$ of	finite		cou	ntably	infinit	te [unc	count	able	

Name:												
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Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6
(5 points) Let the "touches" rela explain why it is,		(a,b)T(c,d)	if and	donly	if $a =$	d or b	= c.					
Solution: To $(2,3)T(3,4)$, but if	his relation is no not $(1,2)T(3,4)$.	t transitive.	Cons	sider (1,2), (2,3), a	and (3	3,4).	Γhen	1, 2	T(2,	3) and
(10 points) Ch	neck the (single)	oox that bes	t chai	racteri	zes eac	h item	1.					
-	ntegers p and q and q and q and q if $gcd(p,q) >$	*	${ m tr}$	rue [fals	se _	√				
saucepan last	identical marbles Saturday. 143 rbles this size wi	is			bound ound oi	<u> </u>	√		actly ot a l	7 Dound	lon	
$\forall x \in \mathbb{N}, \text{ if } x < (\pi \text{ is the famil})$	-10 , then $x = \pi$ iar constant.)	 tru	e v	/	false		u	ndefin	ıed			
$f: \mathbb{N}^2 \to \mathbb{R}$ $f(p,q) = pq$		onto		n	ot onto) \[′	not	a fur	nction		
A - B = A	- B	or all sets A				true	for so	ome se	ets A	\ and	В	$\sqrt{}$

Name:_

NetID:

Lecture: \mathbf{A}

2 3 Discussion: Thursday Friday 9 **10** 11 **12** 1 6 4 5

(5 points) Suppose that $f: \mathbb{N} \to \mathbb{N}$ is such that f(n) = n!. Give a recursive definition of f **Solution:**

f(0) = 1, and f(n) = n f(n-1) for n > 1.

You could also have used f(n+1) = (n+1)f(n) for $n \ge 0$.

(10 points) Check the (single) box that best characterizes each item.

Dividing a problem of size n into k subproblems, each of size n/m, has the best big- Θ running time when

k < m

 \mathbf{B}

km = 1

How many ways can I choose 6 bagels from among 8 varieties, if I can have any number of bagels from any type?

6!2!

 $\frac{14!}{9!5!}$

The running time of mergesort is recursively defined by T(1) = d and T(n) =

2T(n-1) + c2T(n/2) + c 2T(n-1) + cn2T(n/2) + cn

1

The chromatic number of a full 3-ary tree

< 3

can't tell

 ≤ 2

 $\{\{a,b\},c\} = \{a,b,c\}$

true

false