

Name: \_\_\_\_\_

NetID: \_\_\_\_\_ Lecture:    A    B

Discussion:    Monday & Wednesday    1:30    2:30

1. (5 points) State the negation of the following claim, moving all negations (e.g. “not”) so that they are on individual predicates.

For every tiger  $k$ , if  $k$  is orange, then  $k$  is large and  $k$  is not friendly.

**Solution:** There is a tiger  $k$  such that  $k$  is not large or  $k$  is friendly, but  $k$  is orange.

2. (5 points) State the contrapositive of the following claim, moving all negations (e.g. “not”) so that they are on individual predicates.

For every tiger  $k$ , if  $k$  is orange, then  $k$  is large and  $k$  is not friendly.

**Solution:** For every tiger  $k$ , if  $k$  is not large or  $k$  is friendly, then  $k$  is not orange.

3. (5 points) Find all integer solutions to the equation  $2p^2 + 5p = 3$ . Show your work.

**Solution:** Since  $2p^2 + 5p = 3$ ,  $2p^2 + 5p - 3 = 0$ . Factoring the lefthand side, we get  $(p - \frac{1}{2})(2p + 6) = 0$ . So  $p$  must be either  $\frac{1}{2}$  or  $-3$ . But  $\frac{1}{2}$  is not an integer. So  $p = -3$ .

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1. (5 points) Simplify, showing your work.

$$25 \times 2^{-3 \log_2(5)} =$$

**Solution:**  $25 \times 2^{-3 \log_2(5)} = 25 \times (2^{\log_2(5)})^{-3} = 25 \times 5^{-3} = 25 \times \frac{1}{125} = \frac{1}{5}$

2. (10 points) Check the (single) box that best characterizes each item.

Shorthand for the set of integers.

 $\mathbb{J}$  ☐ $\mathbb{N}$  ☐ $\mathbb{W}$  ☐ $\mathbb{Z}$  ☒

If U. Illinois is in Paris,  
then  $\pi < 0$ .

true ☒false ☐undefined ☐ $[-3.4]$ -3 ☐-4 ☒3.4 ☐undefined ☐ $\neg(p \wedge \neg q) \equiv \neg p \vee q$ true ☒false ☐ $p \rightarrow q \equiv \neg p \rightarrow \neg q$ true ☐false ☒