

Name:\_\_\_\_\_

NetID:\_\_\_\_\_ Lecture: A

Discussion: Monday &amp; Wednesday 1:30 2:30

$$A = \{(x, y) \in \mathbb{Z}^2 \mid y = x^2 + 5x + 9\}$$

$$B = \{(a, b) \in \mathbb{Z}^2 \mid a \leq 2\}$$

$$C = \{(p, q) \in \mathbb{Z}^2 \mid q > 20\}$$

Prove that  $A \subseteq B \cup C$ .

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1. (4 points)  $A = \{\text{apple, maple, elm}, \emptyset\}$        $B = \{\text{tree, oak}, \emptyset\}$   
 $A \cap B =$

$$\{(p, q) : p \in \mathbb{Z}, q \in \mathbb{Z}, \text{ and } pq = 6\} =$$

2. (4 points) Check the (single) box that best characterizes each item.

$A \cap B \subseteq A$	true for all sets A and B	<input type="checkbox"/>	true for some sets A and B	<input type="checkbox"/>
	false for all sets A and B	<input type="checkbox"/>		

$\forall x \in \mathbb{N}$ , if  $x^2 < -3$ , then  $x > 1000$ .      true ☐      false ☐      undefined ☐

3. (7 points) In  $\mathbb{Z}_{13}$ , find the value of  $[7]^{18} + [7]^4$ . You must show your work, keeping all numbers in your calculations small. **You may not use a calculator.** You must express your final answer as  $[n]$ , where  $0 \leq n \leq 12$ .