

NAME \_\_\_\_\_

MIDTERM EXAM

ECE 451

October 15, 2014

12:00 – 12:50 p.m.

Instructions: Write your name and section where indicated. Show all work. Indicate the units of your answers.

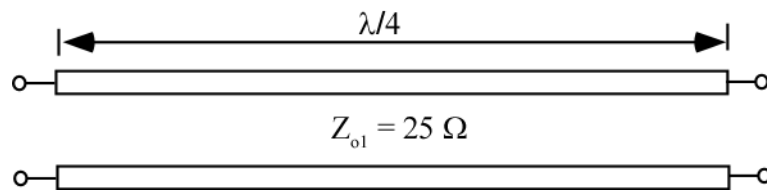
Mason's non-touching loop rule:

$$T = \frac{P_1 \left[ 1 - \sum L(1)^{(1)} + \sum L(2)^{(1)} - \dots \right] + P_2 \left[ 1 - \sum L(1)^{(2)} + \sum L(2)^{(2)} - \dots \right] + \dots}{1 - \sum L(1) + \sum L(2) - \sum L(3) + \dots}$$

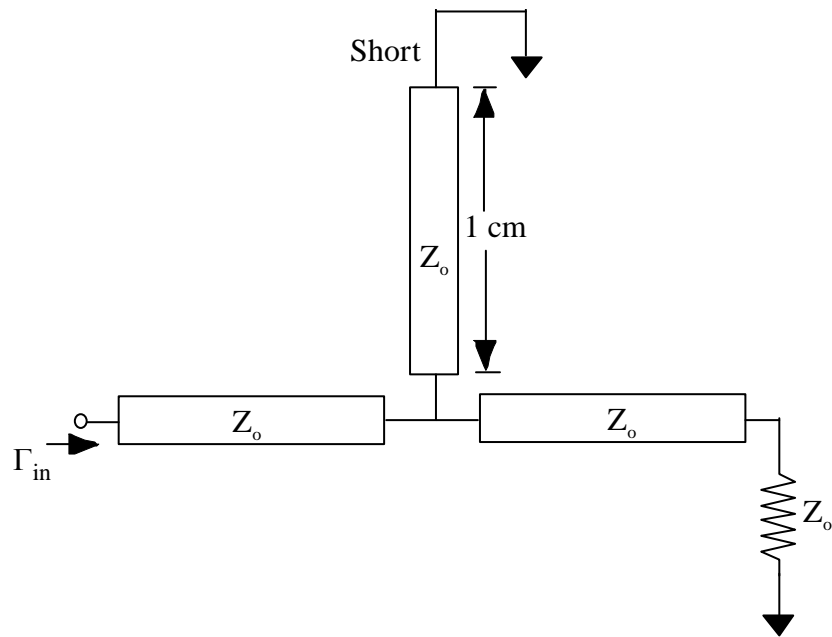
Problem 1 (25 pts)	Problem 2 (25 pts)	Problem 2 (25 pts)	Problem 2 (25 pts)	Total (100 pts)

1. A transmission line of characteristic impedance  $Z_o$ , length  $d$  and propagation constant  $\beta$  is terminated with an open.
  - (a) Find the input impedance.
  - (b) Draw a rough sketch of  $Z_{in}/Z_o$  for  $\beta d$  ranging from 0 to  $\pi$  and label the frequency bands where the transmission line looks capacitive and where it looks inductive.
  - (c) At what frequencies does this open transmission line look like a short circuit?

2. For the transmission line shown below, write the scattering parameter matrix as measured on a 50- $\Omega$  network analyzer.



3. For the circuit shown below (lab student unknown), the transmission lines use air as dielectric. What is the lowest frequency for which  $\Gamma_{\text{in}} = 0$ ? (Use  $Z_0$  as your reference impedance).



4. A lossless transmission line has the following per unit length parameters:  $L = 80 \text{ nH}\cdot\text{m}^{-1}$ ,  $C = 200 \text{ pF}\cdot\text{m}^{-1}$ . Consider a traveling wave on the transmission line with a frequency of 1 GHz.

- (a) What is the attenuation constant?
- (b) What is the phase constant?
- (c) What is the phase velocity?
- (d) What is the characteristic impedance of the line?
- (e) Now consider that the dielectric is replaced by a dielectric with  $\epsilon_r = 1$  (or air). The capacitance per unit length of the line is now  $C(\text{air}) = 50 \text{ pF}\cdot\text{m}^{-1}$ . What is the effective relative dielectric constant of the line?