

Name \_\_\_\_\_

(circle your TA discussion section)

- ▷ **AD1**, TR 1:00-1:50, Sarah Son      ▷ **AD2**, TR 1:00-1:50, Daniel Hockensmith  
 ▷ **AD4**, TR 1:00-1:50, Sogol Jahanbekam      ▷ **AD5**, TR 2:00-2:50, Daniel Hockensmith  
 ▷ **AD7**, TR 3:00-3:50, Nersés Aramyan      ▷ **AD8**, MW 11:00-12:50, Austin Rochford  
 ▷ **AD9**, MW 9:00-10:50, Ben Reiniger
- 

- Sit in your assigned seat (shown below).
  - Do not open this test booklet until I say *START*.
  - Turn off all electronic devices and put away all items except a pen/pencil and an eraser.
  - You must show sufficient work to justify each answer.
  - While the test is in progress, we will not answer questions concerning the test material.
  - Quit working and close this test booklet when I say *STOP*.
  - Quickly turn in your test to me or a TA and show your Student ID.
- 

263	264	265	266	267	268	269	270	•	271	272	273				278	279	•	280	281	282	283	284	285	286	287
240	241	242	243	244	245	246	•	247	248	249	250	251	252	253	254	255	•	256	257	258	259	260	261	262	
217	218	219	220	221	222	223	•	224	225	226	227	228	229	230	231	232	•	233	234	235	236	237	238	239	
194	195	196	197	198	199	200	•	201	202	203	204	205	206	207	208	209	•	210	211	212	213	214	215	216	
171	172	173	174	175	176	177	•	178	179	180	181	182	183	184	185	186	•	187	188	189	190	191	192	193	
148	149	150	151	152	153	154	•	155	156	157	158	159	160	161	162	163	•	164	165	166	167	168	169	170	
•	•	•	•	•	•	•	•	139	140	141	56	143	144	13	146	147	•	•	•	•	•	•	•	•	
116	117	118	119	120	121	122	•	123	124	125	126	127	132	145	130	131	•	16	133	134	135	136	137	138	
93	94	95	96	97	98	99	•	100	101	102	103	128	105	106	107	108	•	109	110	111	112	113	114	115	
70	71	72	73	74	75	76	•	77	78	79	80	81	82	83	84	85	•	86	87	88	89	90	91	92	
47	48	49	50	51	52	53	•	54	55	104	57	58	59	60	61	62	•	63	64	65	66	67	68	69	
24	25	26	27	28	29	30	•	31	32	33	34	35	36	37	38	39	•	40	41	42	43	44	45	46	
1	2	3	4	5	6	7	•										•	17	18	19	20	21	22	23	

FRONT OF ROOM – 314 Altgeld Hall

1. (8 points) Determine an appropriate linear approximation of the function  $f(x) = \sqrt{x}$  and use it to approximate  $\sqrt{26.3}$ . Write your answer in decimal form.

2. (6 points) Precisely state *Rolle's Theorem*.

3. (8 points) Evaluate the following limit. Be sure to use proper notation throughout your evaluation of this limit. Simplify your answer.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \frac{17}{4n} - \frac{5k}{2n^2} \right)$$

4. (12 points) Suppose  $f$  is an even function,  $g$  is an odd function, and  $f$  and  $g$  are each integrable on the interval  $[-3, 3]$ . Given that  $\int_0^3 f(x) dx = 5$  and  $\int_0^3 g(x) dx = 4$ , evaluate the following definite integrals.

(a)  $\int_3^0 g(x) dx$

(b)  $\int_3^3 f(x) dx$

(c)  $\int_{-3}^3 (2f(x) + 4g(x)) dx$

(d)  $\int_{-3}^3 (4 + (g(x))^5) dx$

5. (9 points each) Evaluate the following definite integrals. Simplify each answer.

$$(a) \int_{\pi/3}^{\pi/2} (12 + 6 \sin x) \, dx$$

$$(b) \int_0^2 (6x^2 + 3e^{-x}) \, dx$$

6. (8 points each) Evaluate the following indefinite integrals.

$$(a) \int \frac{6x^3 + 4x^2 + 5x}{x^2} dx$$

$$(b) \int \frac{1}{x\sqrt{\ln x}} dx$$

$$(c) \int \tan^5 x \sec^4 x \, dx$$

7. (6 points) Evaluate the following indefinite integral.

$$\int x^2 \sqrt{x+1} \, dx$$

8. (6 points each) The intersection points on the graphs of  $f(x) = x^2 + 2$  and  $g(x) = 3x + 6$  occur at  $x = -1$  and at  $x = 4$ . Let  $\mathbf{R}$  be the finite region bounded by the graphs of  $f(x)$  and  $g(x)$ . Set up, but do not evaluate, definite integrals which represent the given quantities. Use proper notation.

(a) The area of  $\mathbf{R}$ .

(b) The volume of the solid obtained when  $\mathbf{R}$  is revolved around the vertical line  $x = 10$ .

(c) The volume of the solid obtained when  $\mathbf{R}$  is revolved around the  $x$ -axis.

**Students – do not write on this page!**

1. (8 points) \_\_\_\_\_

2. (6 points) \_\_\_\_\_

3. (8 points) \_\_\_\_\_

4. (12 points) \_\_\_\_\_

5a. (9 points) \_\_\_\_\_

5b. (9 points) \_\_\_\_\_

6a. (8 points) \_\_\_\_\_

6b. (8 points) \_\_\_\_\_

6c. (8 points) \_\_\_\_\_

7. (6 points) \_\_\_\_\_

8a. (6 points) \_\_\_\_\_

8b. (6 points) \_\_\_\_\_

8c. (6 points) \_\_\_\_\_

**TOTAL (100 points)** \_\_\_\_\_