

1. (8 points) Evaluate the following indefinite integrals.

(a) $\int \sin x \, dx$

(b) $\int \cos x \, dx$

(c) $\int \frac{1}{x} \, dx$

(d) $\int e^x \, dx$

(e) $\int \sec^2 x \, dx$

(f) $\int \csc^2 x \, dx$

(g) $\int \sec x \tan x \, dx$

(h) $\int \csc x \cot x \, dx$

2. (8 points) Evaluate the definite integral. Simplify your answer.

$$\int_{-2}^2 (x^{25} + 4x^5 + 3x^2 + 5) \, dx$$

3. (8 points) Evaluate the definite integral. Simplify your answer.

$$\int_0^{1/2} \frac{6}{4x^2 + 1} dx$$

4. (8 points) Evaluate the indefinite integral.

$$\int 10x^9 (x^5 + 3)^{100} dx$$

5. (8 points) Evaluate the indefinite integral.

$$\int x^3 \tan^2(x^4) dx$$

6. (10 points) Evaluate the indefinite integral.

$$\int \sin^3 x \cos^{15} x dx$$

7. (10 points) Evaluate the following limit. Be sure to use proper notation throughout your evaluation of this limit. Simplify your answer.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left(\frac{10k}{n^2} + \frac{3}{n+2} \right)$$

8. (8 points) Let $g(x) = \int_2^{x^3-12x} e^{t^2} dt$. At which value of x does $g(x)$ have a local minimum?

9. (12 points) Let \mathbf{R} be the finite region bounded by the x -axis, the y -axis, and the line $2x + 5y = 10$. Revolve \mathbf{R} around the vertical line $x = 8$ to form a solid. In the following manner, set up but do not evaluate definite integrals which represent the volume of the solid.

(a) Integrate with respect to x .

(b) Integrate with respect to y . (The integrands in parts (a) and (b) should be different.)

10. (10 points) In order to approximate $\sqrt{26.6}$, begin with an initial estimate of $x_1 = 5$ and use Newton's Method to obtain a second estimate x_2 . Simplify your final answer.

11. (10 points) A stone was dropped off a cliff and hit the ground with a speed of 160 ft/s . What is the height of the cliff?

Students – do not write on this page!

1. (8 points) _____

2. (8 points) _____

3. (8 points) _____

4. (8 points) _____

5. (8 points) _____

6. (10 points) _____

7. (10 points) _____

8. (8 points) _____

9. (12 points) _____

10. (10 points) _____

11. (10 points) _____

TOTAL (100 points) _____